

$$1. 8^{x+3} - 14 = 18$$

$$8^{x+3} = 32$$

$$(2^3)^{x+3} = 2^5$$

$$3x+9 = 5$$

$$3x = -4$$

$$x = -\frac{4}{3}$$

$$2. \frac{-2 \log_6 (3x+12)}{-2} = \frac{-8}{-2}$$

$$\log_6 (3x+12) = 4$$

$$6^{\log_6 (3x+12)} = 6^4$$

$$3x+12 = 1296$$

$$3x = 1284$$

$$x = 428 \quad \checkmark \text{ pos. ans.}$$

$$3. e^{3x-5} + 7 = 15$$

$$e^{3x-5} = 8$$

$$\ln e^{3x-5} = \ln 8$$

$$3x-5 = \ln 8$$

$$3x = \ln 8 + 5$$

$$x = \frac{\ln 8 + 5}{3}$$

$$4. \log_2 (4x-6) = \log_2 (7x-30)$$

$$4x-6 = 7x-30$$

$$-6 = 3x-30$$

$$24 = 3x$$

$$x = 8 \quad \checkmark \text{ pos. ans.}$$

$$5. \frac{1}{4} (3^{2x}) = 11$$

$$3^{2x} = 44$$

$$\log_3 3^{2x} = \log_3 44$$

$$2x = \log_3 44$$

$$x = \frac{1}{2} \log_3 44$$

$$6. \log_6 2 + \log_6 (x-5) = 2$$

$$\log_6 [2(x-5)] = 2$$

$$\log_6 (2x-10) = 2$$

$$2x-10 = 6^2$$

$$2x-10 = 36$$

$$2x = 46$$

$$x = 23 \quad \checkmark \text{ pos. ans.}$$

$$7. 16 = 7 \ln (4x-3) - 12$$

$$28 = 7 \ln (4x-3)$$

$$4 = \ln (4x-3)$$

$$e^4 = 4x-3$$

$$e^4 + 3 = 4x$$

$$x = \frac{e^4 + 3}{4} \quad \checkmark \text{ pos. ans.}$$

$$8. 343^{-2x+1} = 49^{x-9}$$

$$(7^3)^{-2x+1} = (7^2)^{x-9}$$

$$-6x+3 = 2x-18$$

$$3 = 8x-18$$

$$21 = 8x$$

$$x = \frac{21}{8}$$

$$9. 7^{3x} = 15$$

$$\log_7 7^{3x} = \log_7 15$$

$$3x = \log_7 15$$

$$x = \boxed{\frac{1}{3} \log_7 15}$$

$$14. -10 + 2e^x = 29$$

$$2e^x = 39$$

$$e^x = \frac{39}{2}$$

$$x = \boxed{\ln\left(\frac{39}{2}\right)}$$

$$10. 14 - \log \frac{1}{2}x = 17$$

$$-\log \frac{1}{2}x = 3$$

$$\log \frac{1}{2}x = -3$$

$$\frac{1}{2}x = 10^{-3}$$

$$\frac{1}{2}x = \frac{1}{1000}$$

$$15. 4 \ln x = 5$$

$$\ln x = \frac{5}{4}$$

$$x = \boxed{e^{5/4}} \quad \checkmark \text{ pos ans}$$

$$x = \boxed{\frac{1}{500}} \quad \checkmark \text{ pos ans}$$

$$16. 3^x + 12 = 8$$

$$3^x = -4$$

$\boxed{\text{no solution}}$

$$11. \ln\left(\frac{3}{5}x + 8\right) = \ln(1-x)$$

$$\frac{3}{5}x + 8 = 1 - x$$

$$\frac{8}{5}x = -7$$

$$x = \boxed{-\frac{35}{8}} \quad \checkmark \text{ pos ans}$$

$$17. 4e^{3x-5} - 14 = 6$$

$$4e^{3x-5} = 20$$

$$e^{3x-5} = 5$$

$$3x - 5 = \ln 5$$

$$3x = \ln 5 + 5$$

$$x = \boxed{\frac{\ln 5 + 5}{3}}$$

$$12. \frac{1}{216} = 36^{x+2}$$

$$6^{-3} = (3^2)^{x+2}$$

$$-3 = 2x + 4$$

$$-7 = 2x$$

$$x = \boxed{-\frac{7}{2}}$$

$$18. 7^{3x} = 14^{x+5}$$

$$\log_{14} 7^{3x} = \log_{14} 14^{x+5}$$

$$3x \cdot \log_{14} 7 = x + 5$$

$$x(3 \log_{14} 7) - x = 5$$

$$x(3 \log_{14} 7 - 1) = 5$$

$$x = \boxed{\frac{5}{3 \log_{14} 7 - 1}}$$

$$13. 3^4 \cdot 3^{-4x-4} = 27$$

$$3^{-4x-4+4} = 27$$

$$3^{-4x} = 27$$

$$3^{-4x} = 3^3$$

$$-4x = 3$$

$$x = \boxed{-\frac{3}{4}}$$

$$19. \log x + \log(x+21) = 2$$

$$\log [x(x+21)] = 2$$

$$\log (x^2 + 21x) = 2$$

$$x^2 + 21x = 10^2$$

$$x^2 + 21x = 100$$

$$x^2 + 21x - 100 = 0$$

$$(x+25)(x-4) = 0$$

$$x = -25, 4$$

$$\boxed{x = 4}$$

$$20. 4(25^{x-8}) - 247 = 253$$

$$4(25^{x-8}) = 500$$

$$25^{x-8} = 125$$

$$(5^2)^{x-8} = 5^3$$

$$2x - 16 = 3$$

$$2x = 19$$

$$\boxed{x = \frac{19}{2}}$$

$$21. \ln(4x-12) + 5 = 7$$

$$\ln(4x-12) = 2$$

$$4x-12 = e^2$$

$$4x = e^2 + 12$$

$$\boxed{x = \frac{e^2 + 12}{4}}$$

$$22. \log_4(3x+14) = \log_4(5x+26)$$

$$3x+14 = 5x+26$$

$$14 = 2x+26$$

$$-12 = 2x$$

$$x = -6 \text{ pos ans?}$$

$$\boxed{\text{NO SOLUTION}}$$

$$\begin{aligned}
 23. \quad & 625^{x-2} = 125^{2x+4} \\
 & (5^4)^{x-2} = (5^3)^{2x+4} \\
 & 4x - 8 = 6x + 12 \\
 & -8 = 2x + 12 \\
 & -20 = 2x \\
 & \boxed{x = -10}
 \end{aligned}$$

$$\begin{aligned}
 24. \quad & \ln(x-4) + \ln(x) = 3 \\
 & \ln(x^2 - 4x) = 3 \\
 & x^2 - 4x = e^3 \\
 & x^2 - 4x - e^3 = 0 \\
 & \frac{4 \pm \sqrt{16 + 4e^3}}{2} = \frac{4 \pm \sqrt{4(4 + e^3)}}{2} \\
 & \frac{4 \pm 2\sqrt{4 + e^3}}{2} \\
 & \boxed{x = 2 + \sqrt{4 + e^3}}, \quad \cancel{2 - \sqrt{4 + e^3}}
 \end{aligned}$$